



# Replicated Abstract Data Types

Kick-off meeting of ConcoRDanT project

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Until now,

**C**ommutative

**R**eplicated

**D**ata

**T**ypes

have been introduced

Since 2006, I proposed

**R**eplicated

**A**bstract

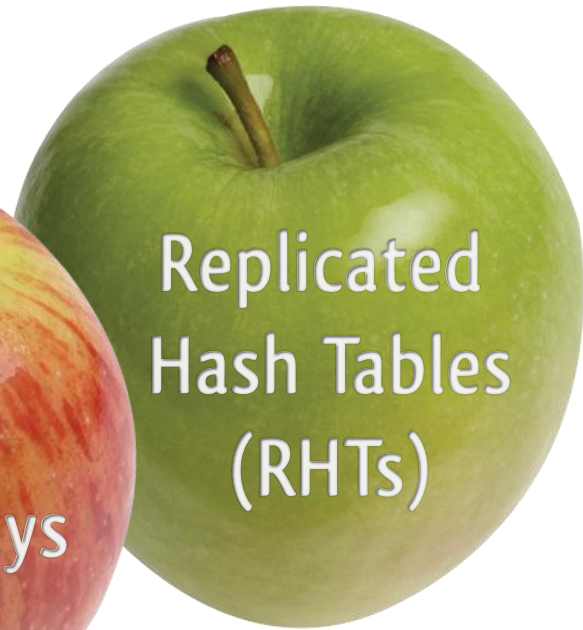
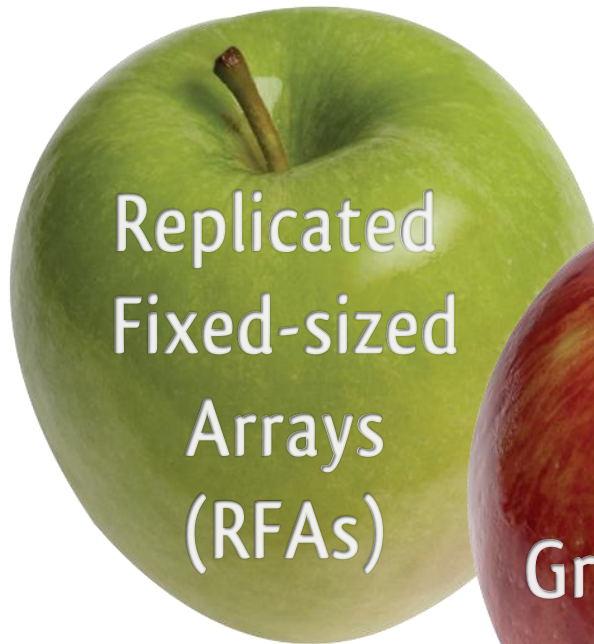
**D**ata

**T**ypes

# Replicated Abstract Data Types (RADTs)

= Replicated Data Structures

+ Optimistic Operations



# Replicated Growable Arrays (RGAs)

= Replicated **Ordered** Objects

+ Optimistic {**Insert**, **Delete**, Update}

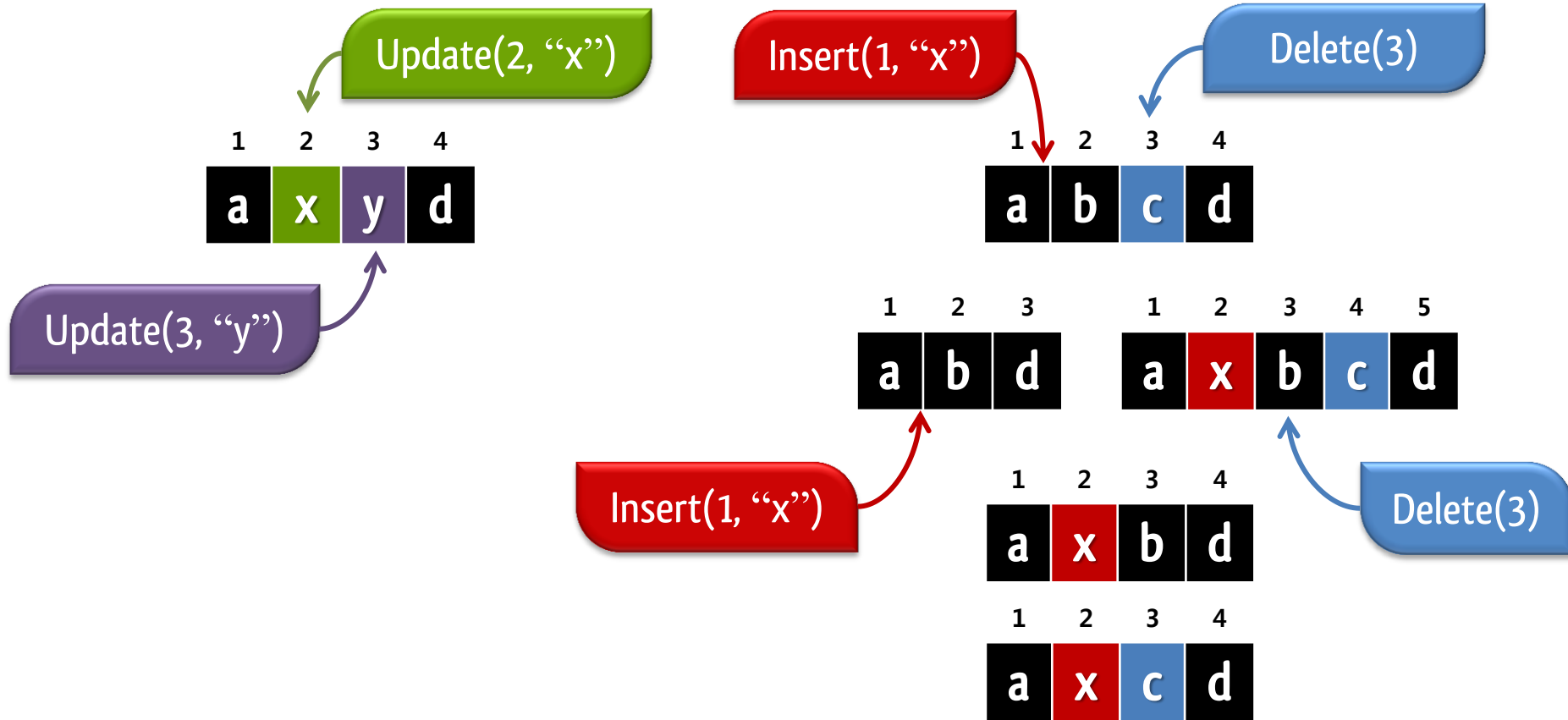


# Concurrent Insert/Delete

more likely

affect (interfere)

each other

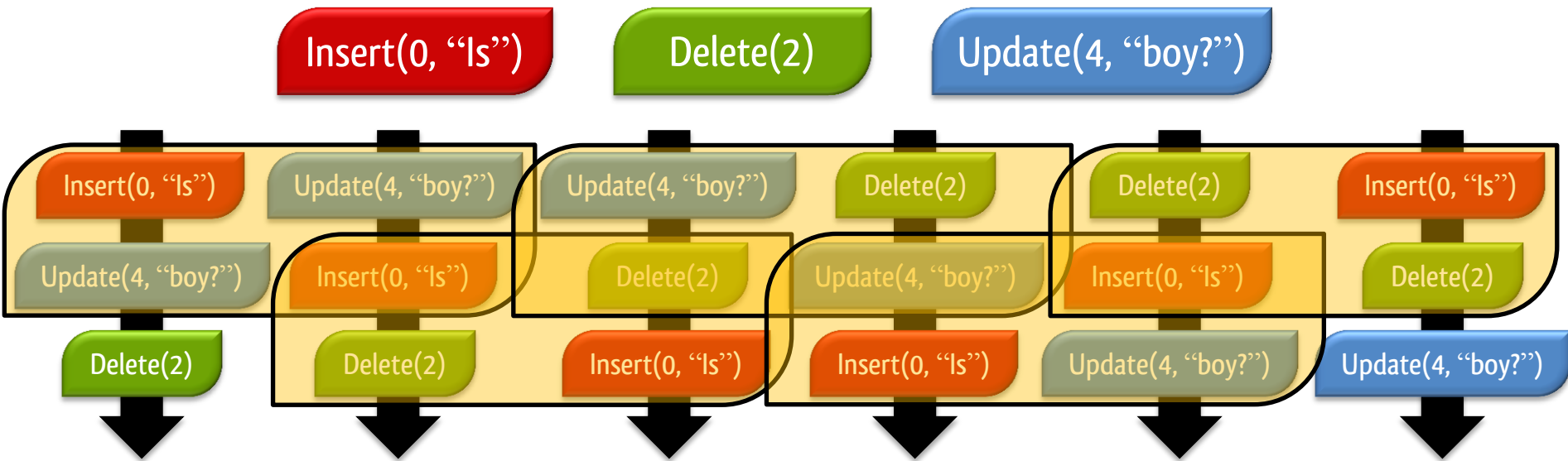


Concurrent Inserts/Deletes

distort the intentions of other operations

# Operation Commutativity

The condition that **every pair** of **concurrent** operations are commutative!!

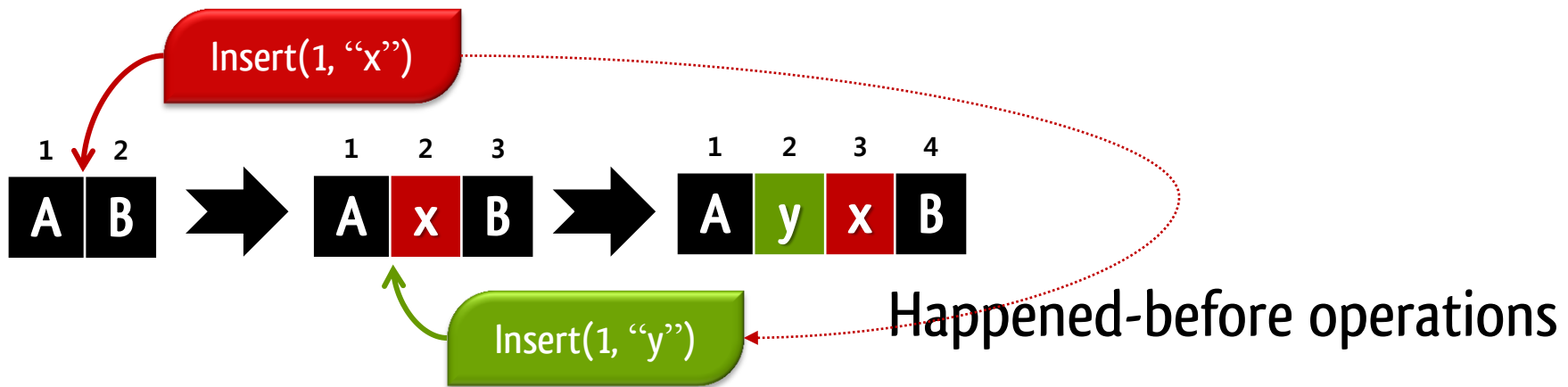


“ It is **not** difficult to make **a pair** of concurrent operations commute ”

“ **But**, it is difficult to make **every pair** of concurrent **Insert/Delete** operations commute ”

# RGAs for Operation Commutativity and Intention

**Precedence** = whose **intention** has higher priority?



The same intentions:

“Insert a new object next to the **1<sup>st</sup>** object”

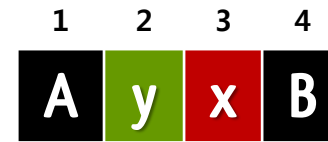
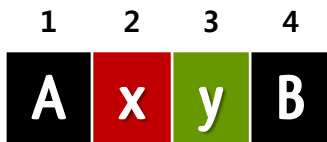
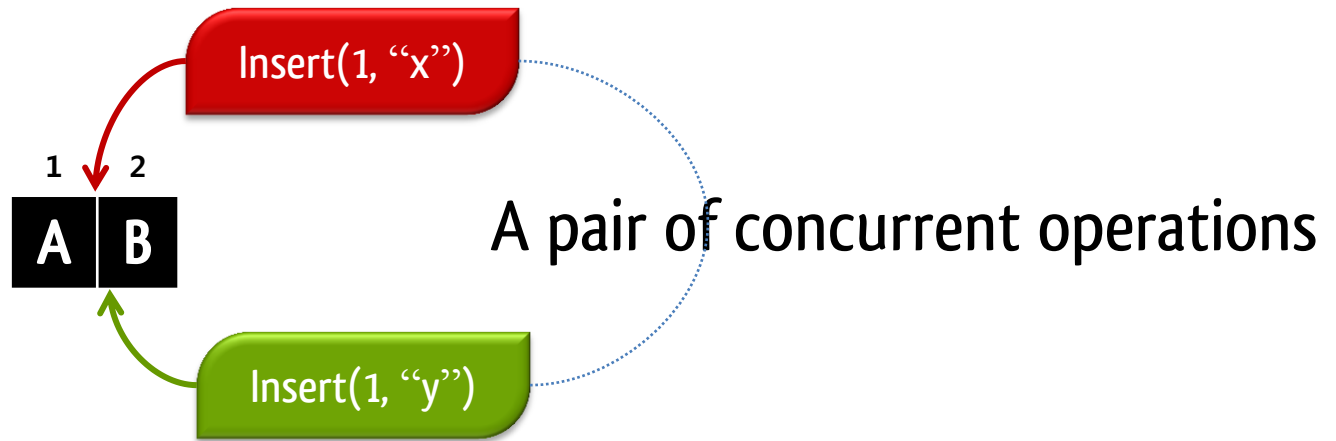
precedence of

`Insert(1, "x")`

<

precedence of

`Insert(1, "y")`



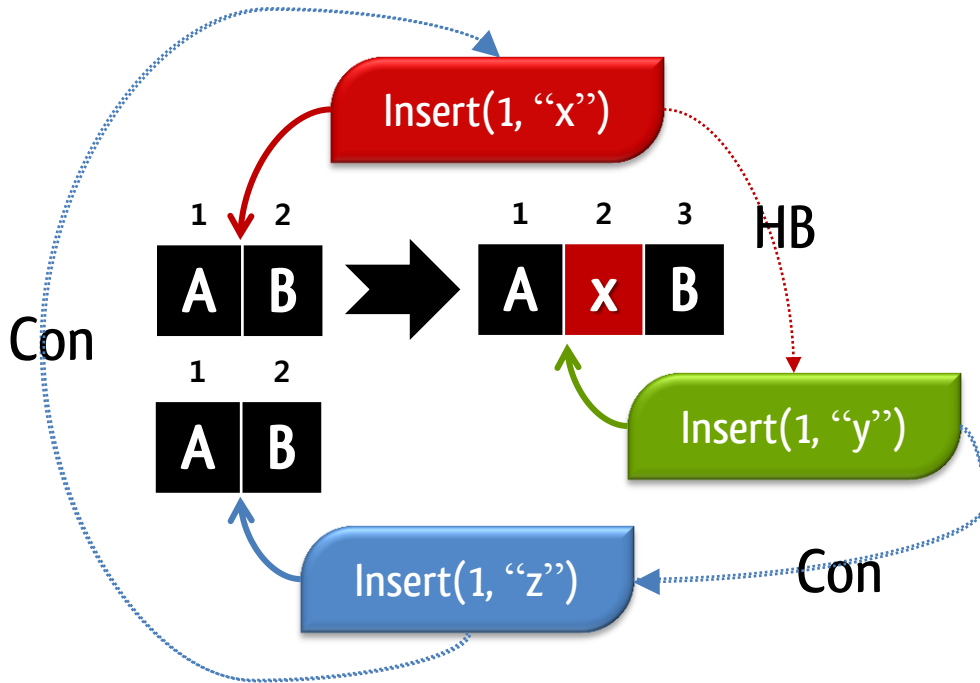
Precedence between a pair of concurrent operations



Define **One** precedence for consistency!!!



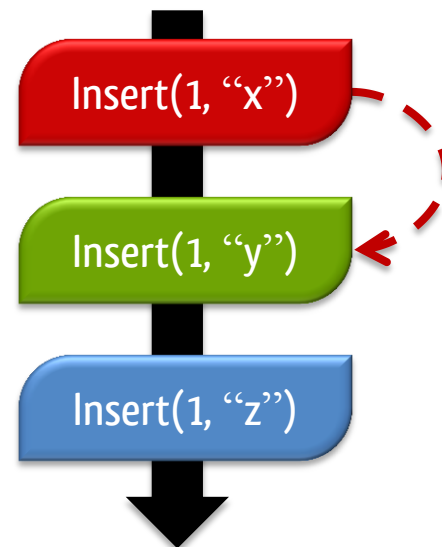
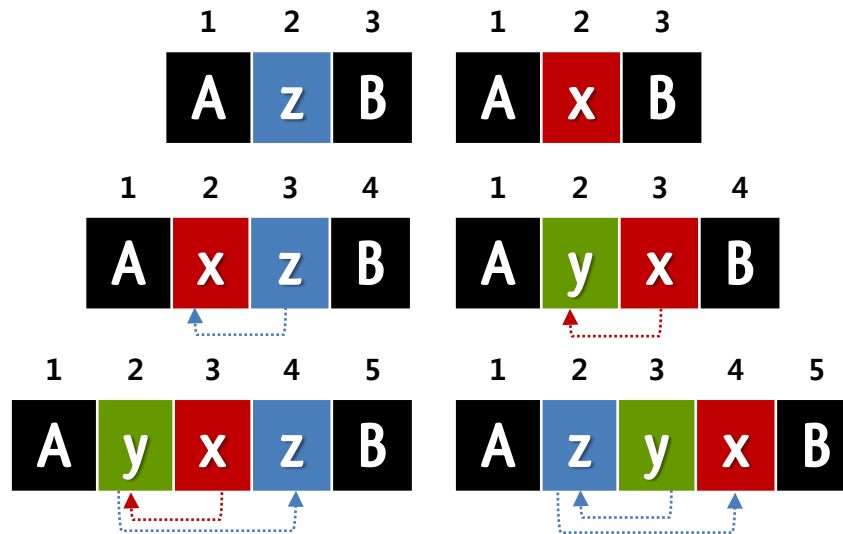
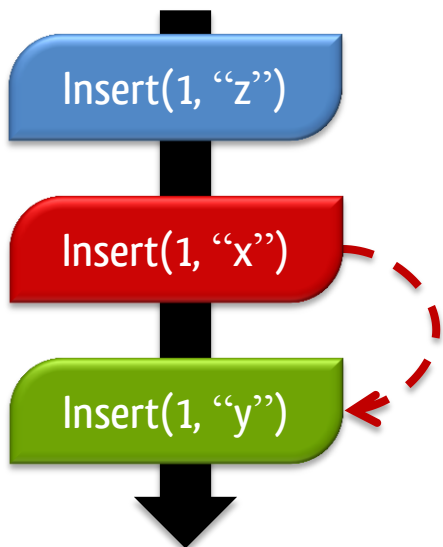
# Precedence among multiple pairs of concurrent operations?



Happened-before operations



Concurrent operations



Insert(1, "x")

<

Insert(1, "y")

Insert(1, "y")

<

Insert(1, "z")

Insert(1, "x")

<

Insert(1, "z")

# Precedence Transitivity (PT)

**Recall**

Allow **every** site to execute operations in a **different** order (Not a total order)

→ Operation Commutativity

Make **a pair** of concurrent operations commute → Precedence

→ Make **every pair** of concurrent operations commute

→ Precedence Transitivity

# Significance of Precedence Transitivity (PT)

Present a solution to achieve operation commutativity

## without

History of operations,

Deriving total order of objects      or      Totally ordered dense indexing scheme

## Operation Commutativity

→ A principle **only** for **concurrent** operations

## Precedence Transitivity

→ A principle for the **relationship** among  
**happened-before** and **concurrent** operations

# S4Vector

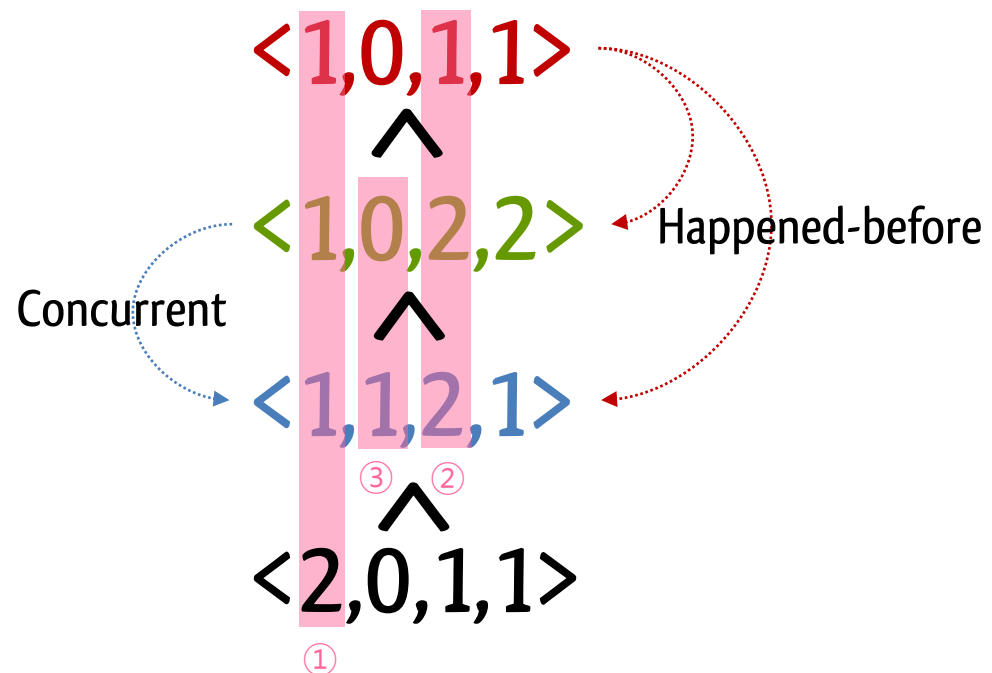
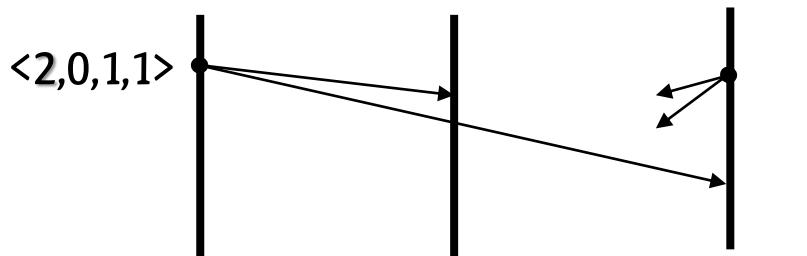
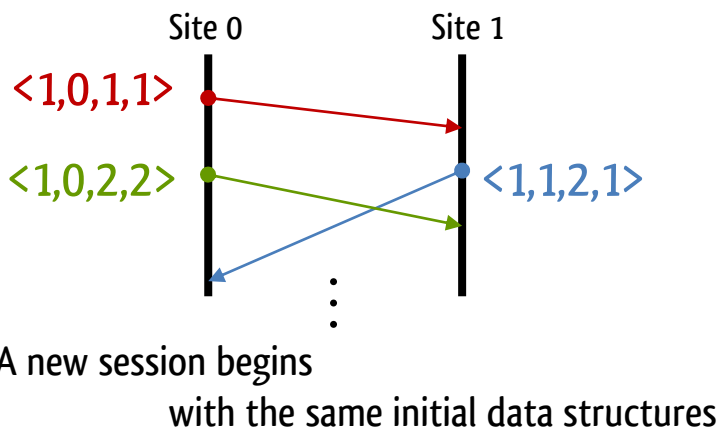
`<int ssn, int sid, int sum, int seq>`

**ssn**: session number

**sid**: site ID

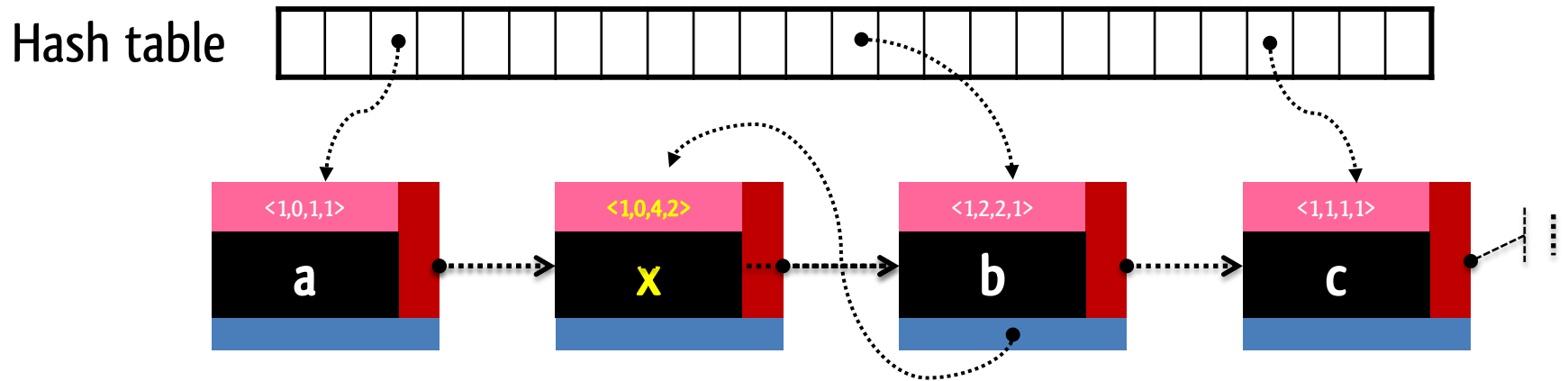
**sum**: sum of a version vector

**seq**: reserved for purging tombstones



# S4Vector Index (SVI) scheme

Adopt a **linked list** with a **hash table**



**Insert(1, "x")** with  $\langle 1,0,4,2 \rangle$   
Local operation

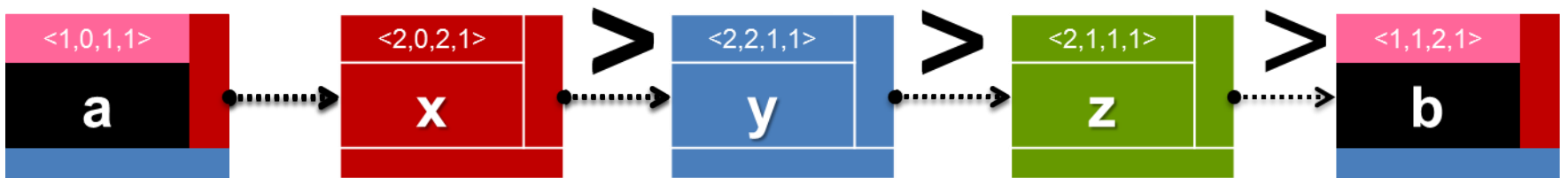
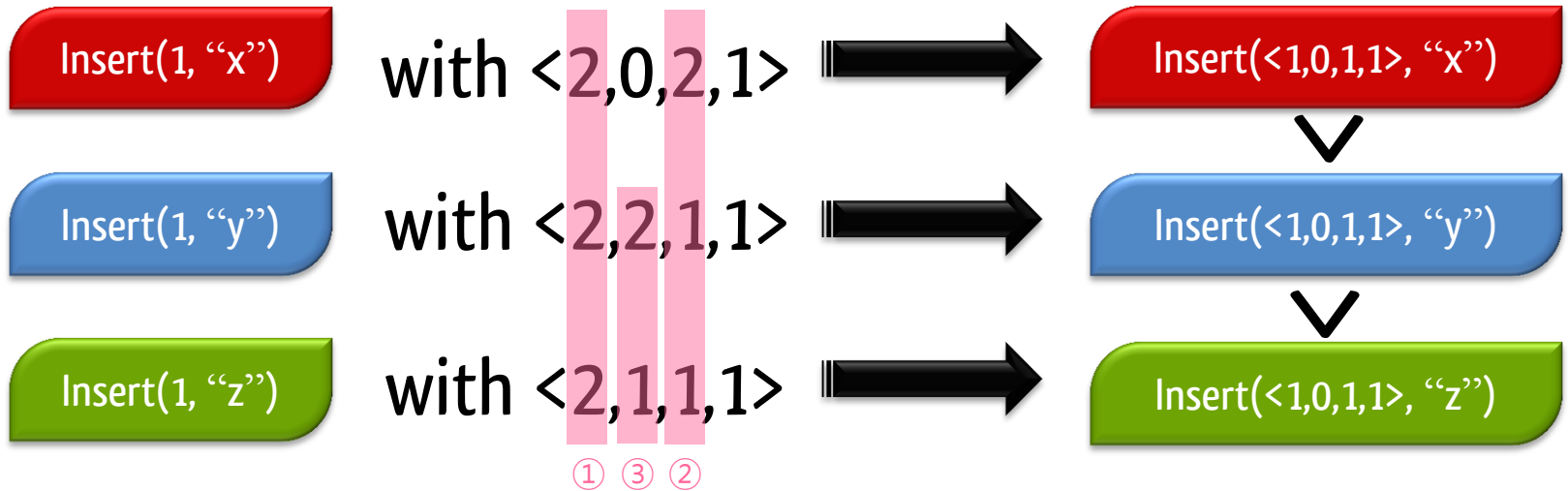
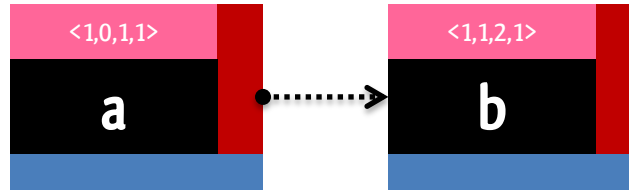


**Insert( $\langle 1,0,1,1 \rangle$ , "x")**  
Remote operation

Preserve **intentions**  
Boost **performance**

of **remote** operations

# Concurrent Inserts



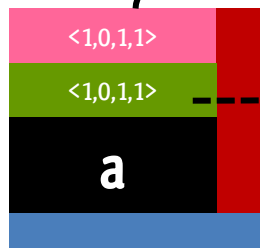
# Summary of RGA implementation

A Delete makes a **tombstone**

Concurrent Inserts

Concurrent Updates

follow **transitivity** of S4Vectors



**Immutable** after an Insert

**Mutable** by Update/Delete

A Delete always wins An update

# Overwhelming performance of RGAs

Algorithms	Local operations	Remote operations
RGAs	$O(N)$ or $\dagger O(1)$	$O(1)$
ABT	$O( H )$	$O( H ^2)$
SDT	$O(1)$	$O( H ^2)$ or $\S O( H ^3)$
TTF	$O(N)$ or $\ddagger O(1)$	$O( H ^2 + N)$
WOOT	$\#O(N^2)$ and $\P O(1)$	$\#O(N^3)$ and $\P O(N)$
Treedoc	$O(\log N)$	$O(\log N)$

N: the number of objects or characters,  
|H|: the number of operations in history buffer,  
 $\dagger$ : local pointer operations,  
 $\ddagger$ : the caret operations,  
 $\S$ : worst-case complexity,  
 $\#$ : WOOT insertion operation,  
 $\P$ : WOOT deletion operation.

Remote operations with 4000 objects

120  $\mu$ S



# 2 sites

# 32 sites

Which performance is important

Remote operations

for Scalability?

Local operations

$O(1)$

Remote operations

Local operations

# RGAs

Consistency of Insert / Delete

Intention preservation

Precedence  
Transitivity

+

SVI scheme

Good performance

Scalability